



# Preliminary reconstructions of the 3D structure of electron bunches based on COTR using two methods

Ze Ouyang

Jan 16<sup>th</sup>, 2025

# Content

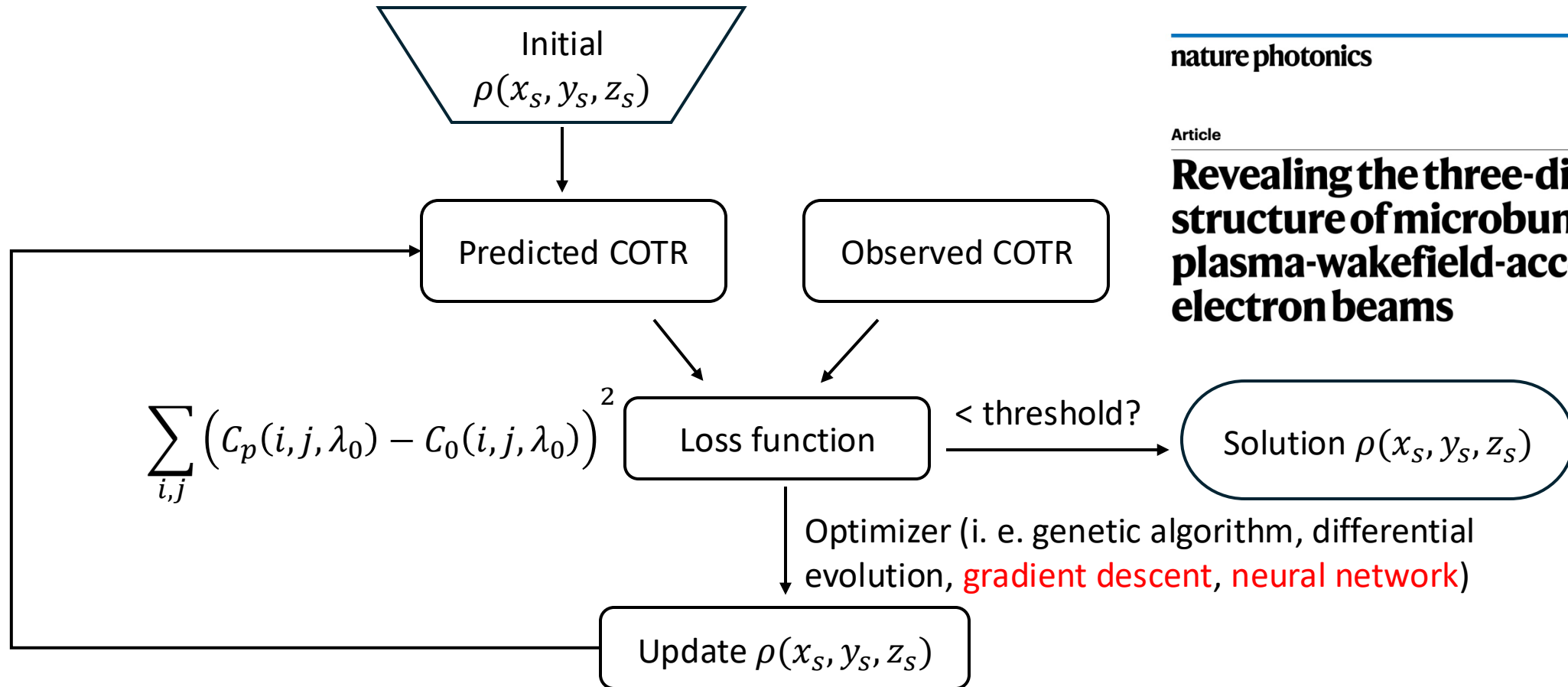
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- Overview of the inverse COTR problem
- Gradient-descent & Generative-neural-network reconstruction
- Several comparison
- Robustness of these two method
- Conclusion & Discussion

# Overview

- Electron bunch  $\rho(x_s, y_s, z_s)$  to COTR  $C(i, j, \lambda_0)$

$$C(i, j, \lambda_0) = \hat{\mathcal{R}}(\rho(x_s, y_s, z_s))$$



ARTICLE

Open Access

## Electro-optic 3D snapshot of a laser wakefield accelerated kilo-ampere electron bunch

Kai Huang<sup>1,2✉</sup>, Zhan Jin<sup>1,2,3</sup>, Nobuhiko Nakai<sup>1,2</sup>, Tomonao Hosokai<sup>2,3</sup> and Masaki Kando<sup>1,2</sup>

nature photonics

Article

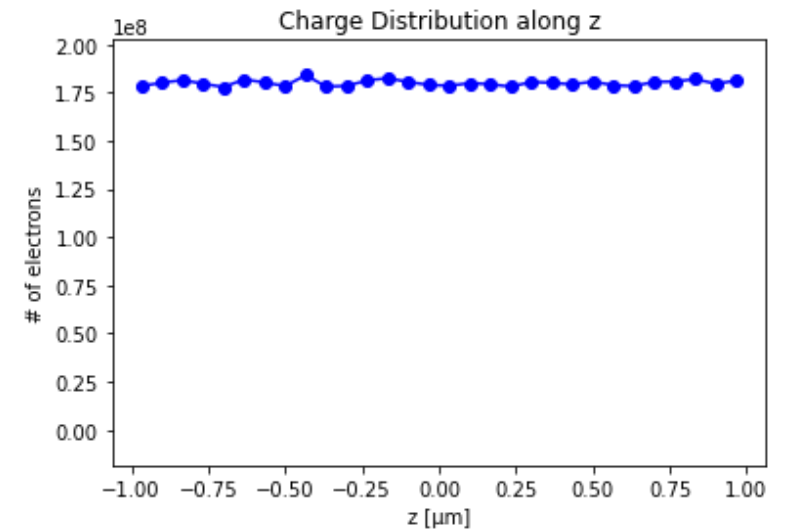
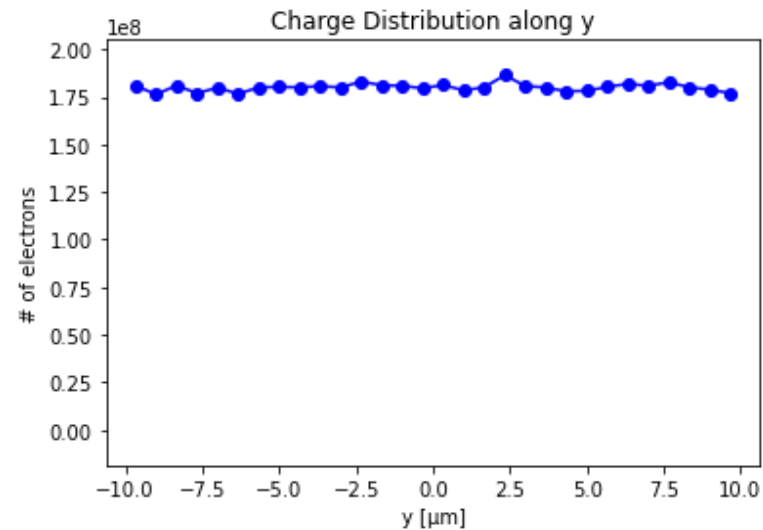
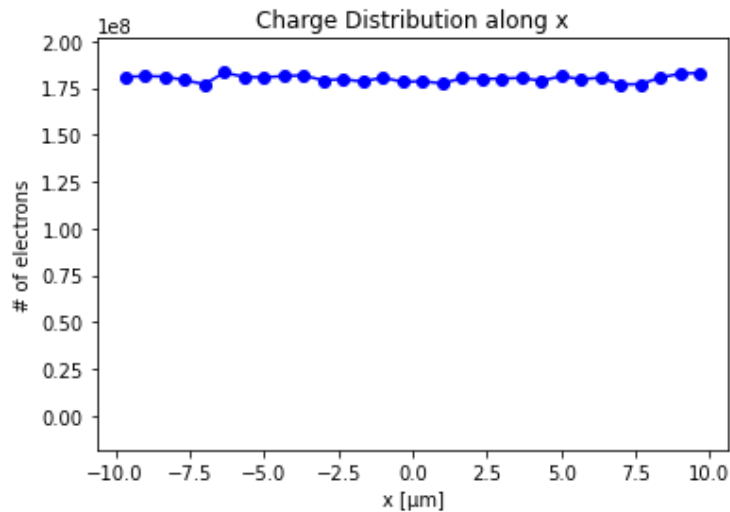
<https://doi.org/10.1038/s41566-023-01000-0>

### Revealing the three-dimensional structure of microbunched plasma-wakefield-accelerated electron beams

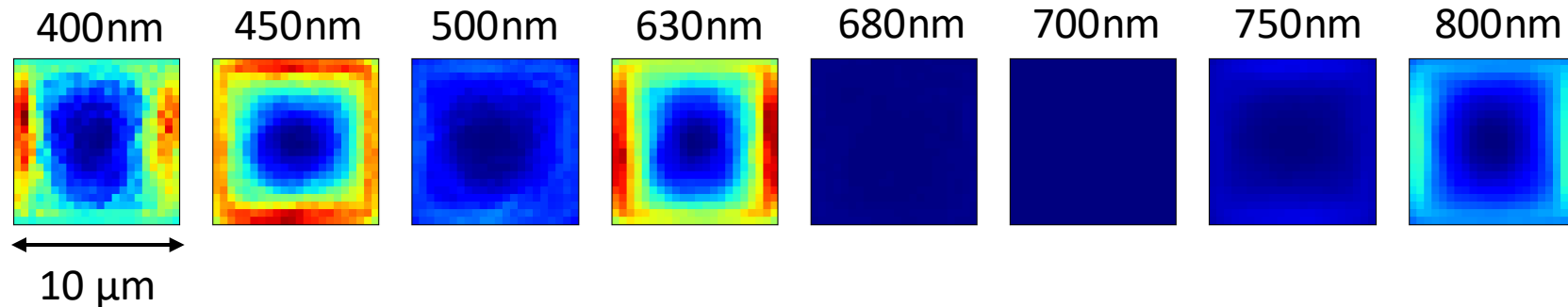
# Description of $\rho(x_s, y_s, z_s)$

- 3D space:  $L_x \times L_y \times L_z$  ( $10\mu\text{m} \times 10\mu\text{m} \times 1\mu\text{m}$ )
- Grids uniformly distributed in this space ( $30 \times 30 \times 30 = 27\text{k}$ )
- Each grid has certain number of electrons,  $5.4\text{e}9$  in total ( $865\text{pC}$ )

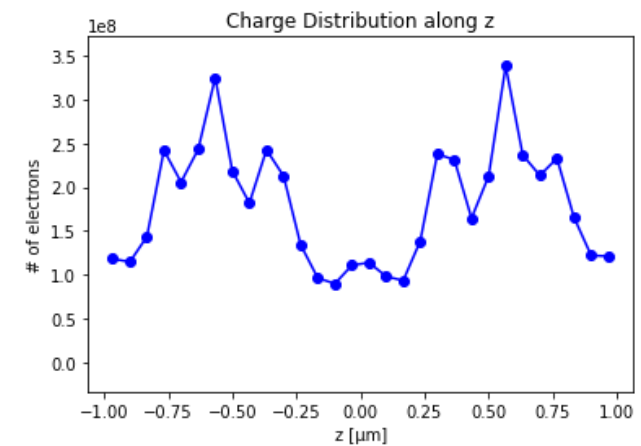
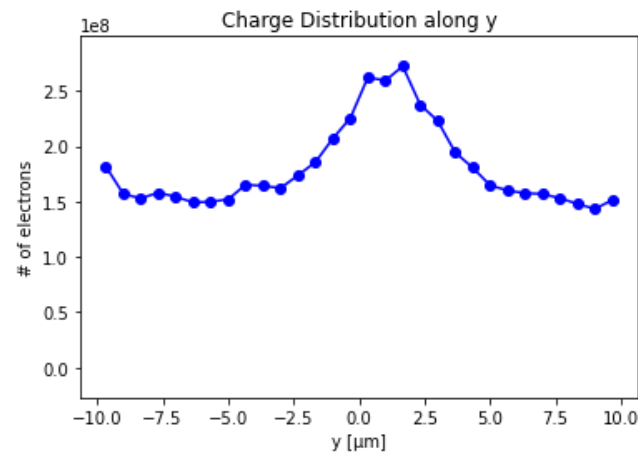
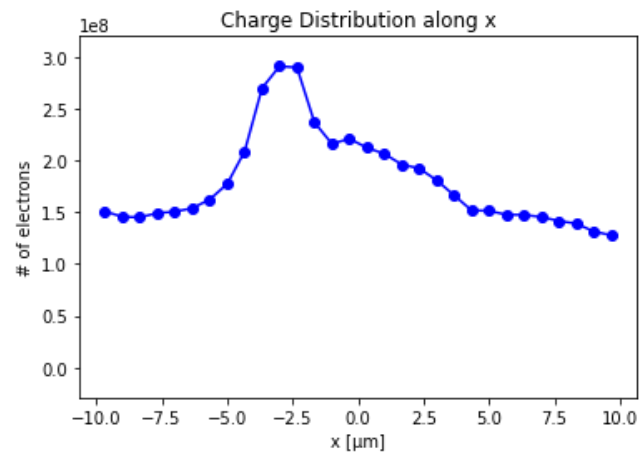
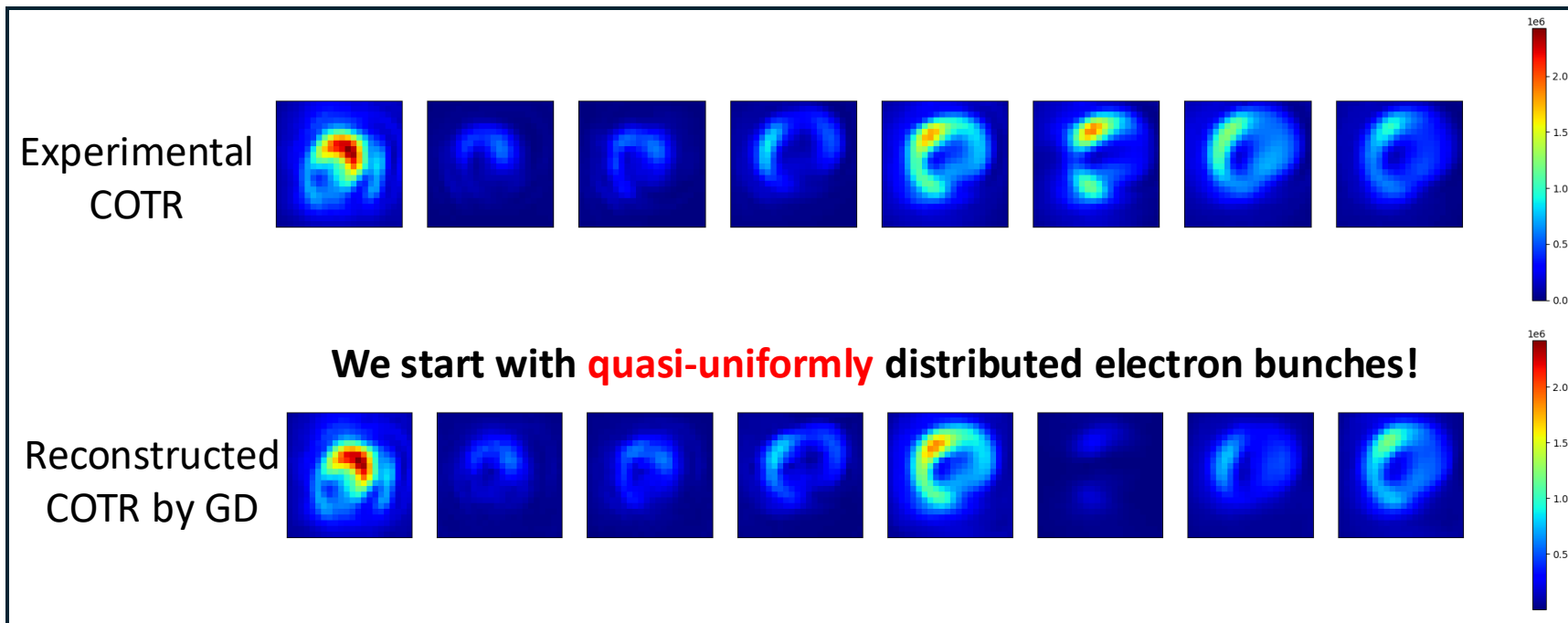
**Task: Find a parameter set (grid charge) that minimizes the lost function**



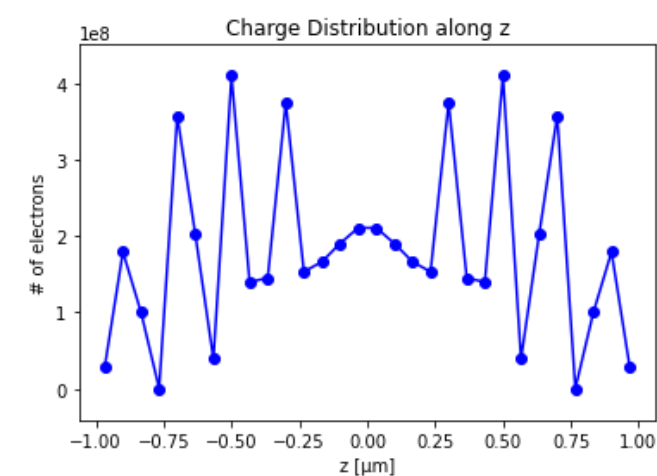
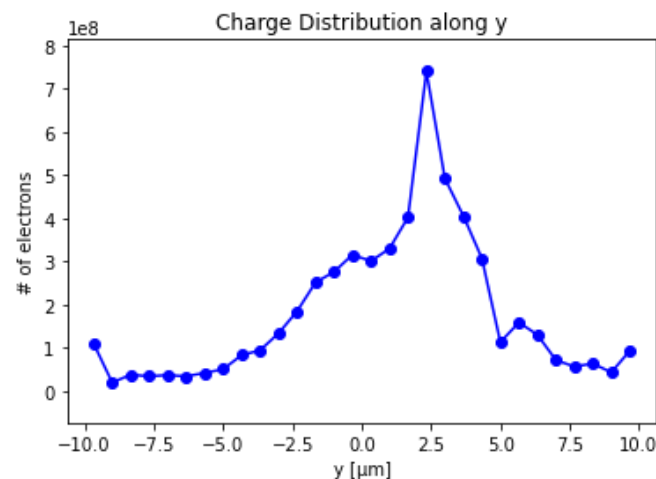
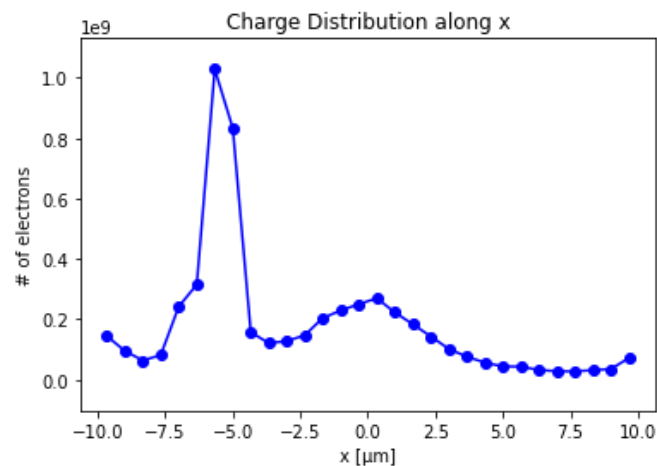
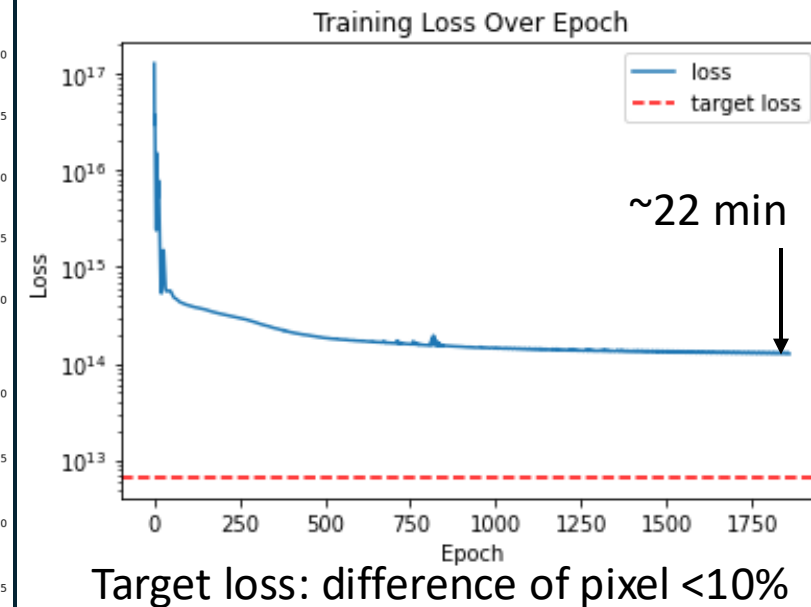
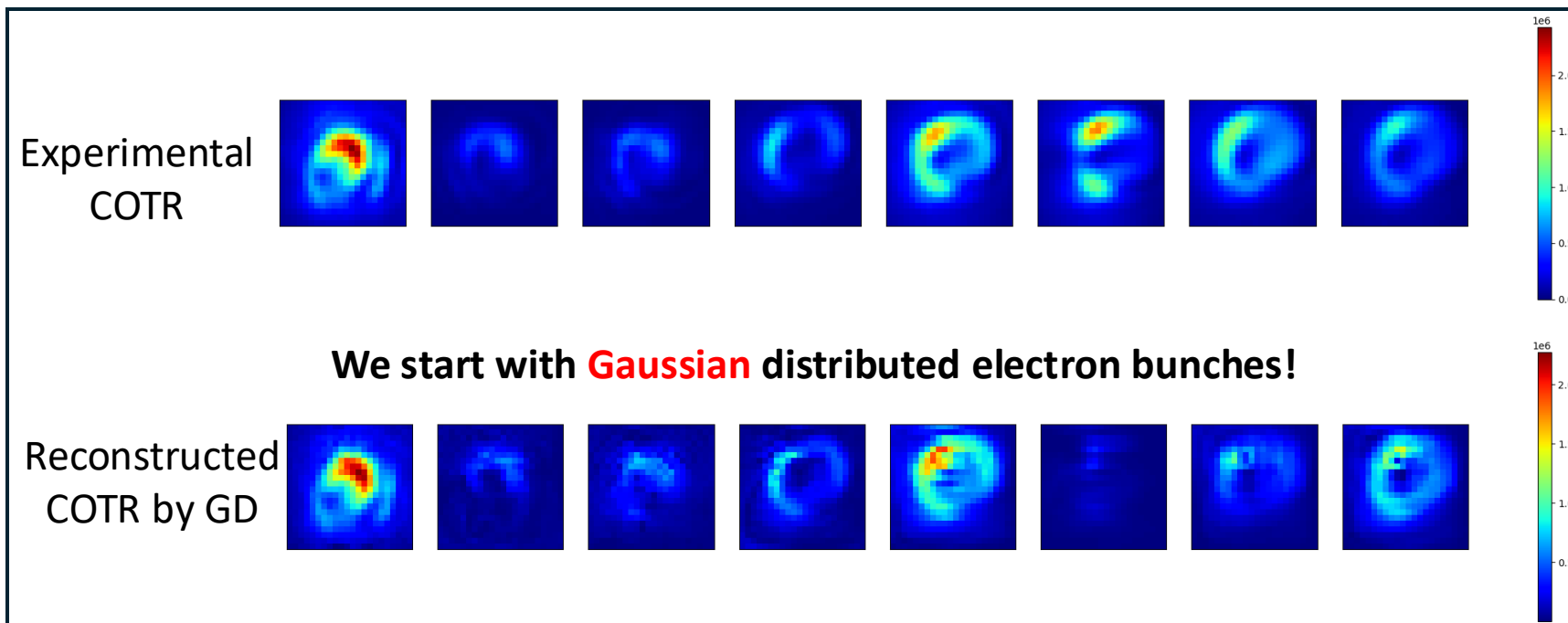
Synthetic COTR



# GD-based reconstruction from uniform $\rho(x_s, y_s, z_s)$



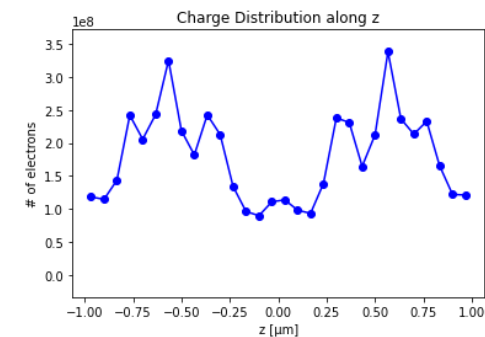
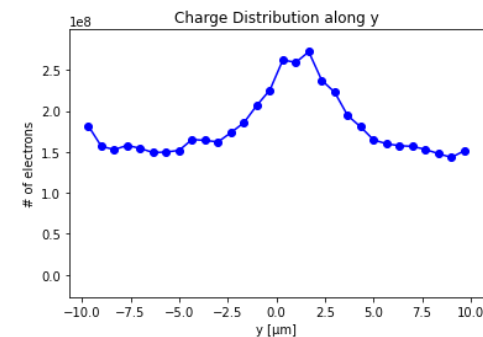
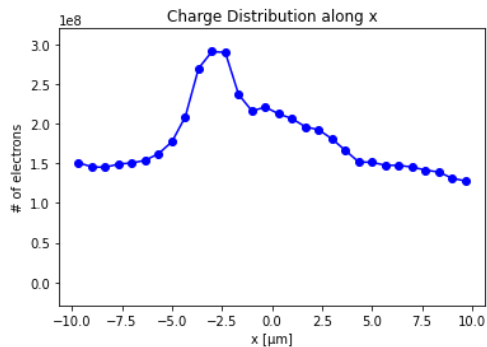
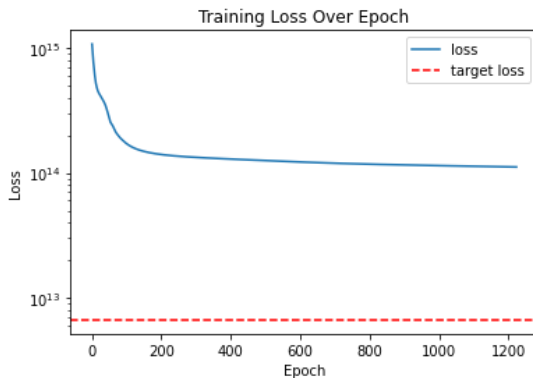
# GD-based reconstruction from Gaussian $\rho(x_s, y_s, z_s)$



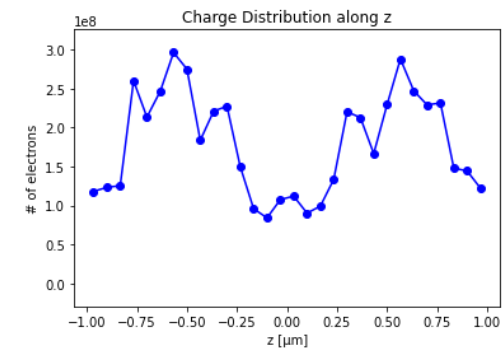
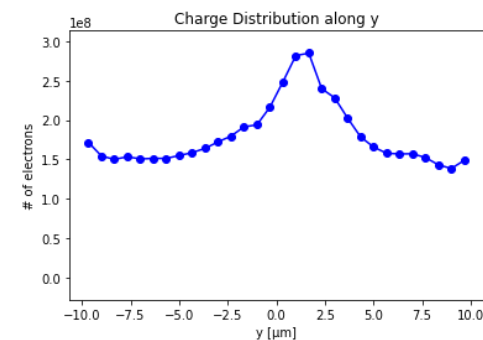
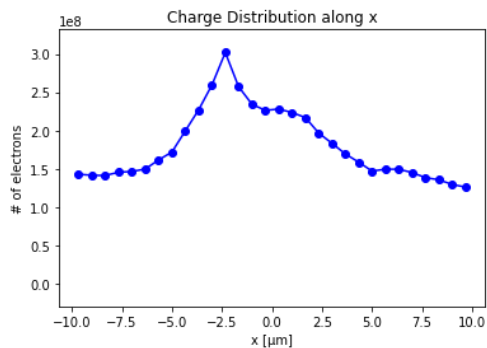
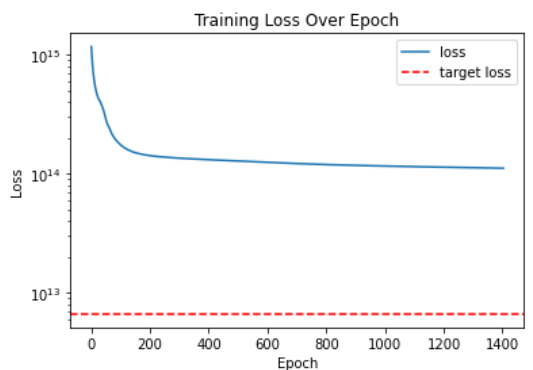
# Uniqueness discussion on GD

We start with **quasi-uniformly** distributed electron bunches!

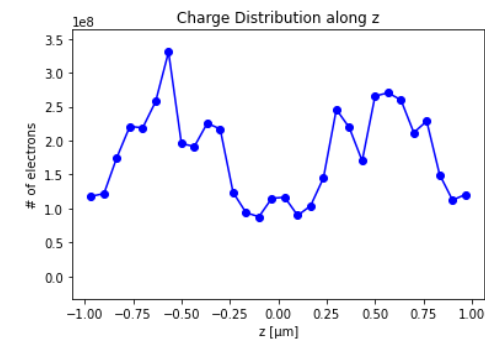
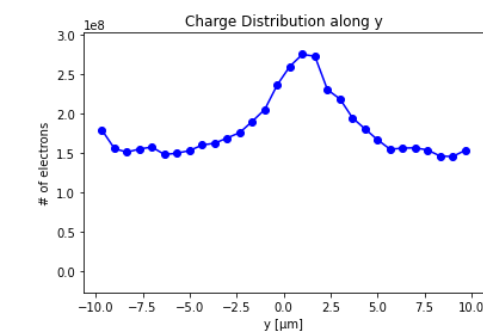
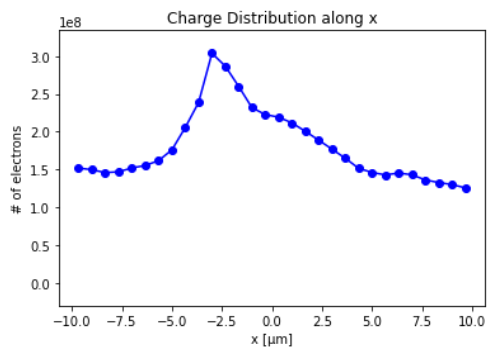
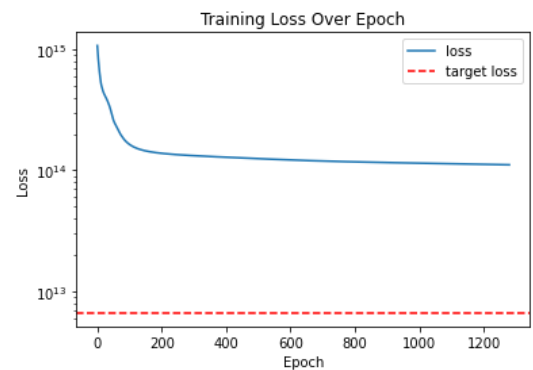
Solution 1



Solution 2



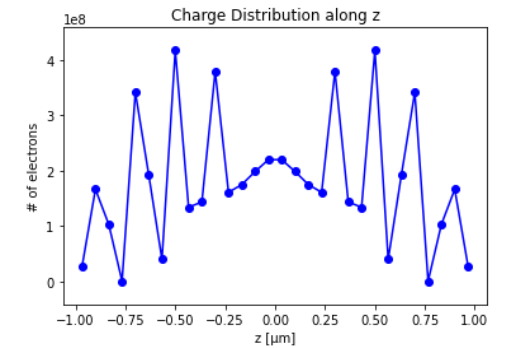
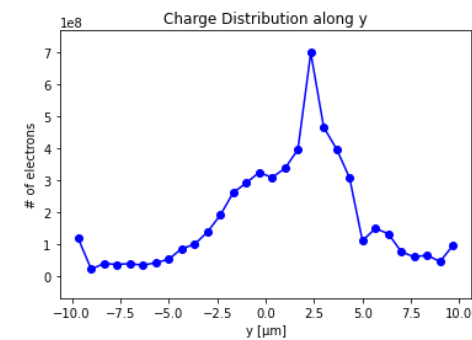
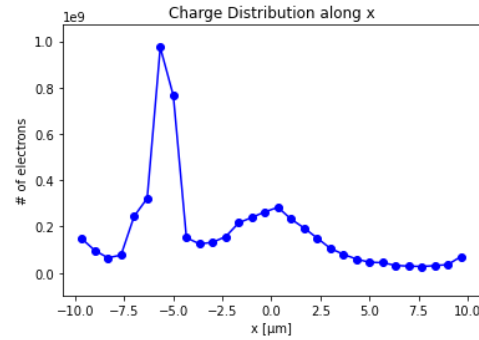
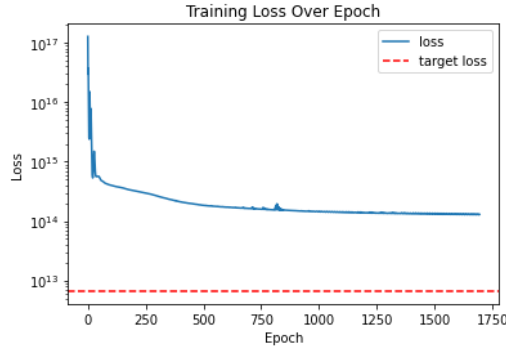
Solution 3



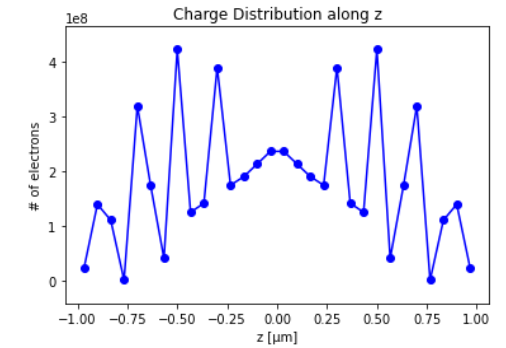
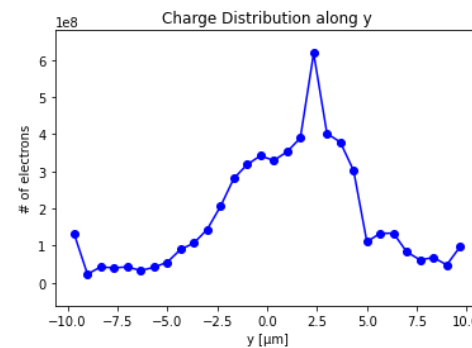
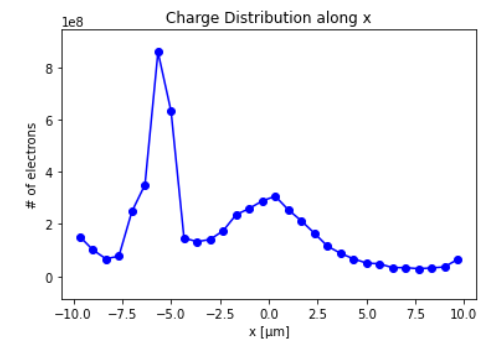
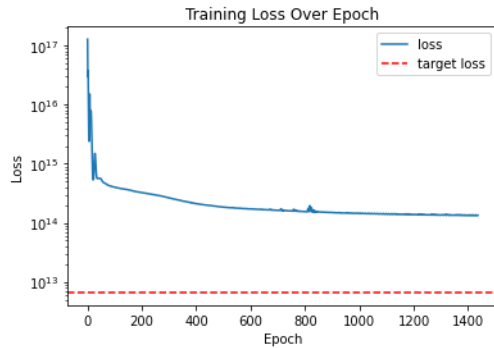
# Uniqueness discussion on GD

We start with **Gaussian** distributed electron bunches!

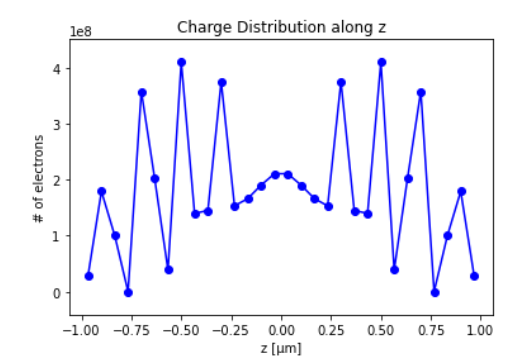
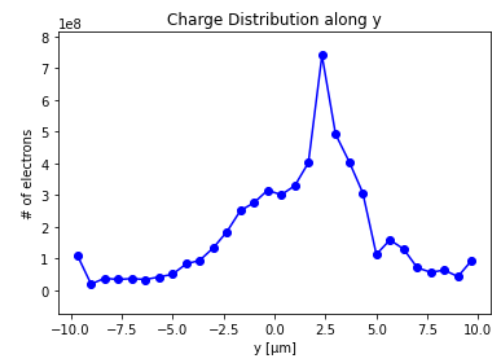
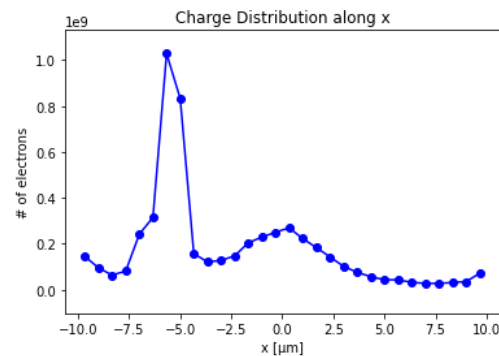
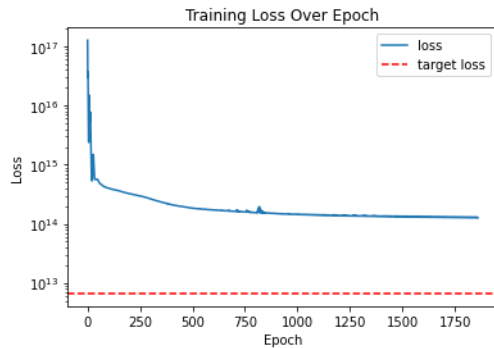
Solution 1



Solution 2



Solution 3

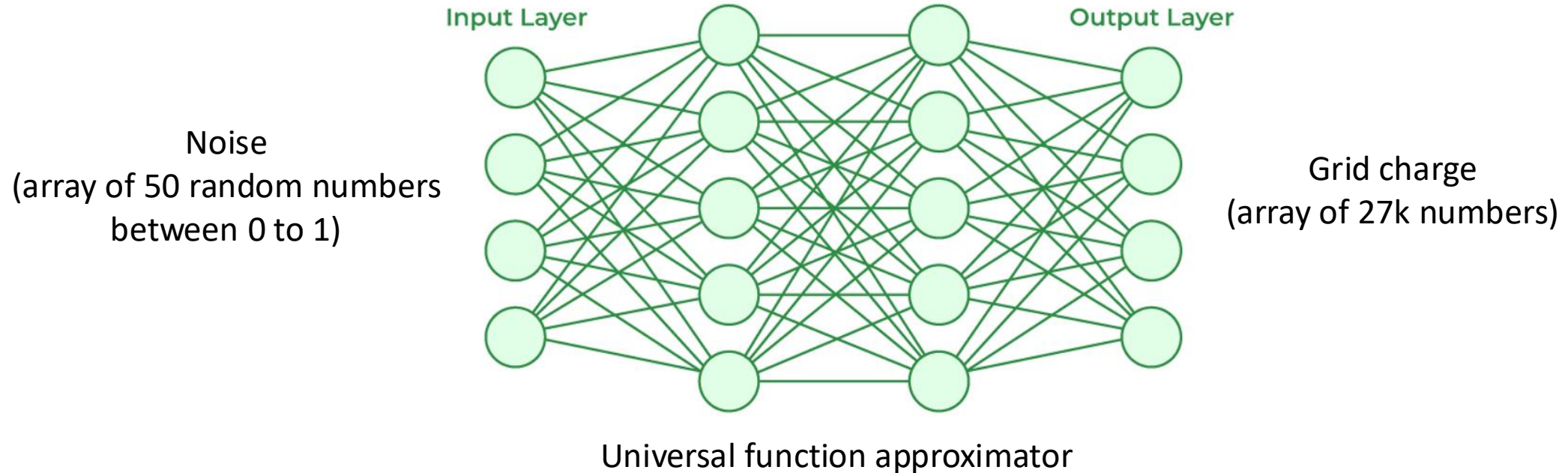




# GNN-based reconstruction

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## Generative Neural Network



- Rather than directly tune the grid charge in the GD method, here we tune the parameters of NN.
- Parameters of NN: Weights, Biases, # of layers, # of neurons per layer, activation function, et al.
- For the case here, we have ~200k parameters of the NN.

# GNN-based reconstruction

PHYSICAL REVIEW LETTERS **130**, 145001 (2023)

## Phase Space Reconstruction from Accelerator Beam Measurements Using Neural Networks and Differentiable Simulations

R. Roussel<sup>1,\*</sup>, A. Edelen, C. Mayes<sup>2</sup>, and D. Ratner<sup>1b</sup>  
*SLAC National Accelerator Laboratory, Menlo Park, California 94025, USA*

PHYSICAL REVIEW ACCELERATORS AND BEAMS **27**, 094601 (2024)

Editors' Suggestion

## Efficient six-dimensional phase space reconstructions from experimental measurements using generative machine learning

Ryan Roussel<sup>1</sup>, Juan Pablo Gonzalez-Aguilera<sup>2</sup>, Eric Wisniewski<sup>3</sup>, Alexander Ody<sup>3</sup>, Wanming Liu<sup>3</sup>, John Power<sup>3</sup>, Young-Kee Kim<sup>2</sup>, and Auralee Edelen<sup>1</sup>

<sup>1</sup>*SLAC National Accelerator Laboratory, Menlo Park, California 94025, USA*

<sup>2</sup>*Department of Physics and Enrico Fermi Institute, University of Chicago, Chicago, Illinois 60637, USA*

<sup>3</sup>*Argonne National Laboratory, Lemont, Illinois 60439, USA*

PHYSICAL REVIEW ACCELERATORS AND BEAMS **27**, 074601 (2024)

## Four-dimensional phase-space reconstruction of flat and magnetized beams using neural networks and differentiable simulations

Seongyeol Kim<sup>1,\*</sup>, Juan Pablo Gonzalez-Aguilera<sup>2,†</sup>, Philippe Piot<sup>1,3</sup>, Gongxiaohui Chen,<sup>1</sup> Scott Doran,<sup>1</sup> Young-Kee Kim,<sup>2</sup> Wanming Liu,<sup>1</sup> Charles Whiteford,<sup>1</sup> Eric Wisniewski,<sup>1</sup> Auralee Edelen,<sup>4</sup> Ryan Roussel<sup>4</sup>, and John Power<sup>1</sup>

This recent paper from our friends at AAC appears relevant to our discussion on Tuesday. MD

**From:** ResearchGate <[no-reply@researchgatemail.net](mailto:no-reply@researchgatemail.net)>

**Date:** Saturday, September 14, 2024 at 3:22 AM

**To:** Downer, Michael <[downer@physics.utexas.edu](mailto:downer@physics.utexas.edu)>

**Subject:** M.C., a recent article cited your research



[M.C., we found a recent citation of your research:](#)

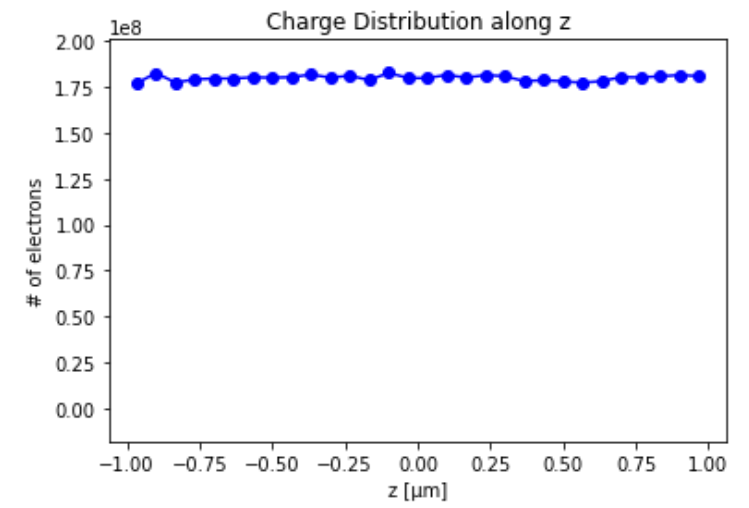
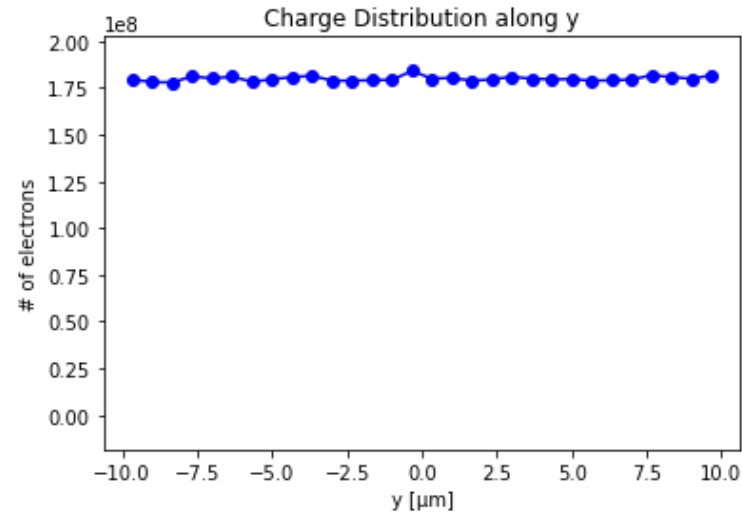
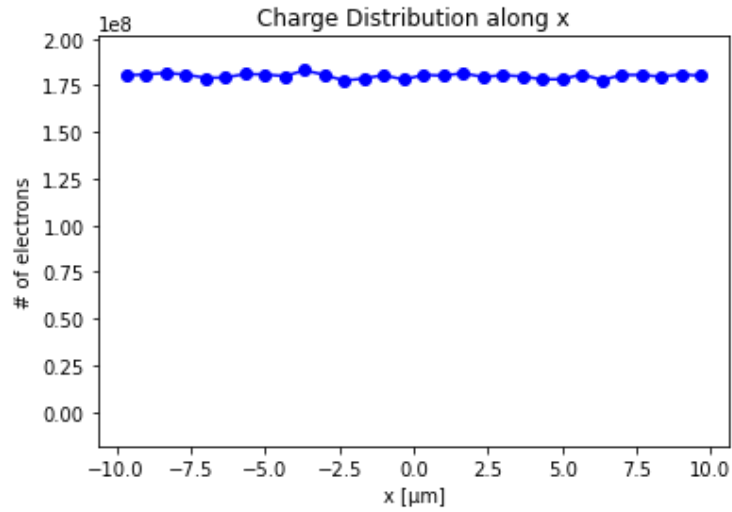
**[Efficient six-dimensional phase space reconstructions from experimental measurements using generative machine learning](#)**

Citing article

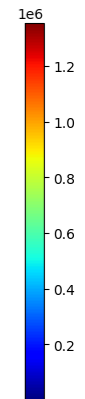
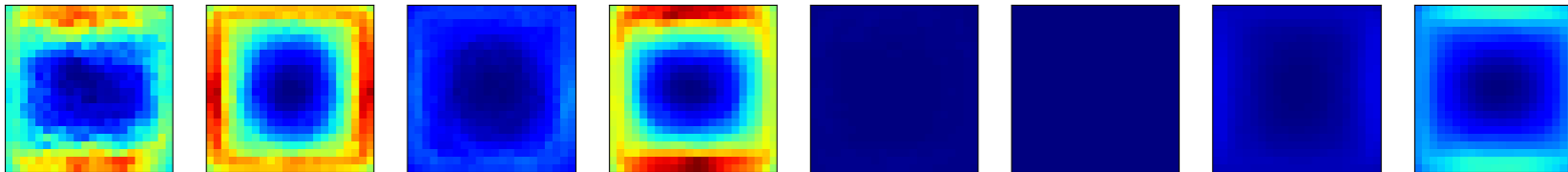
Sep 2024

# GNN-based reconstruction

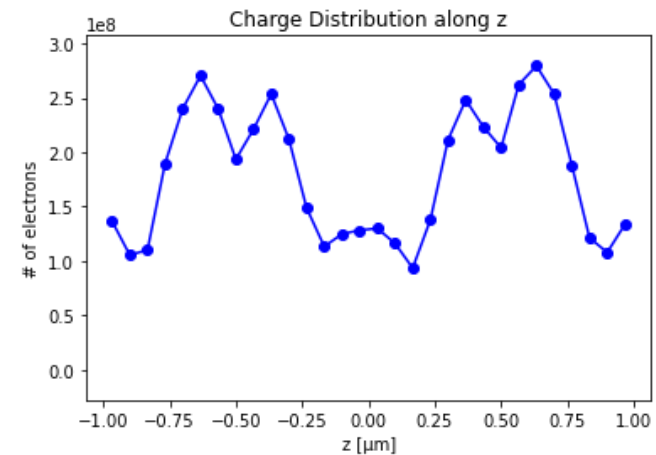
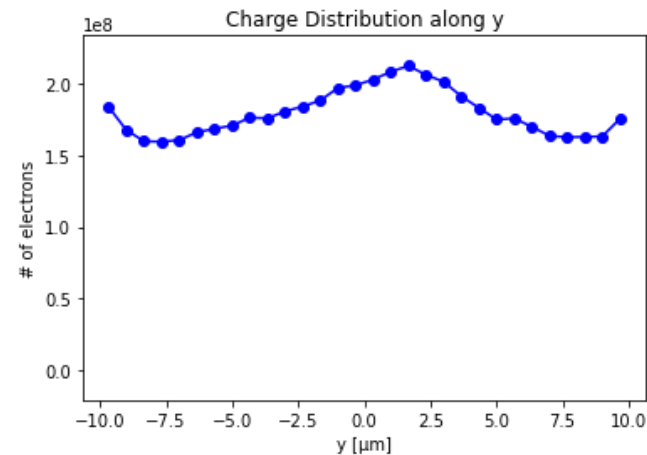
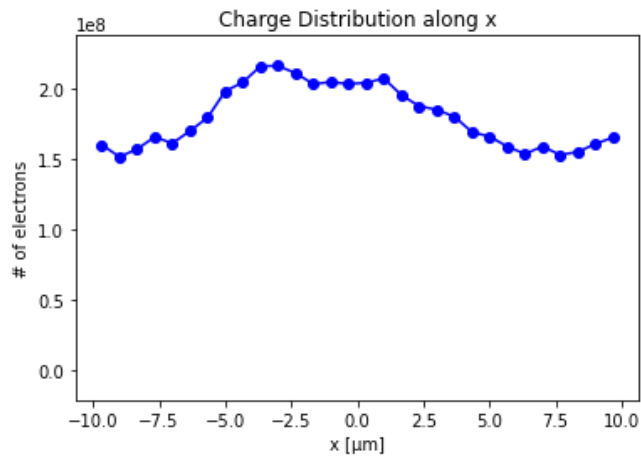
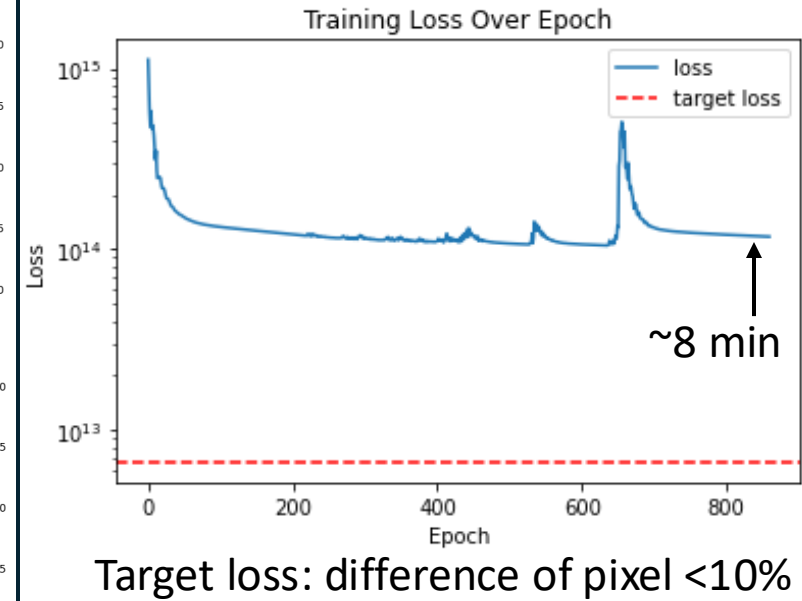
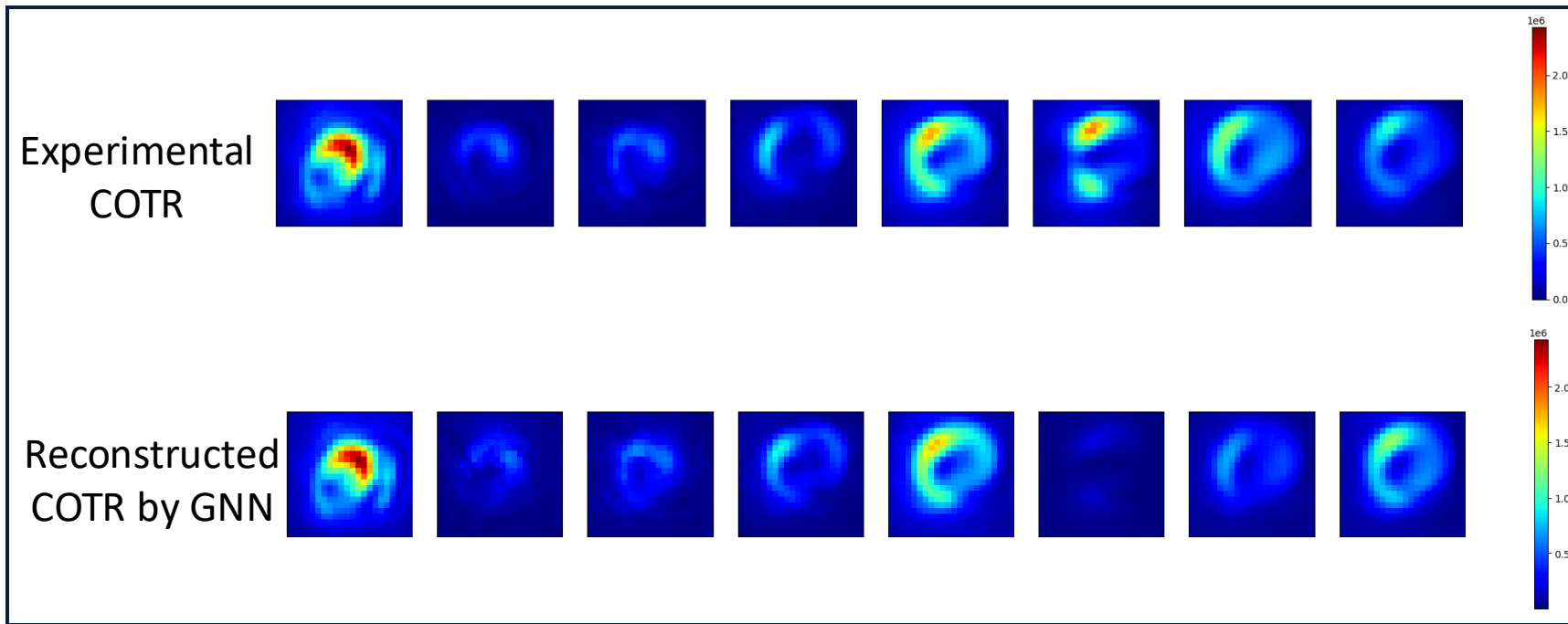
## Initial electron bunches from random noise & initialized GNN



Synthetic  
COTR

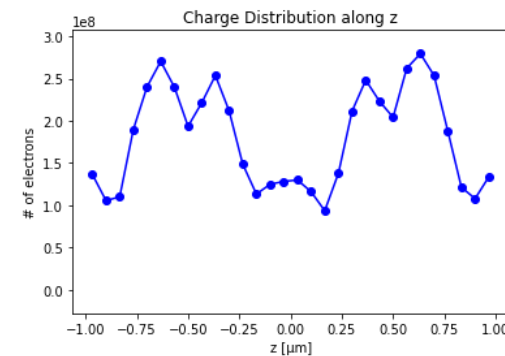
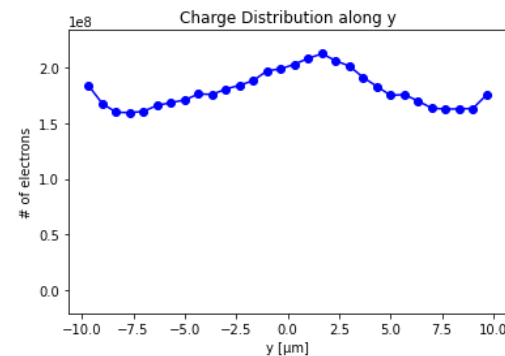
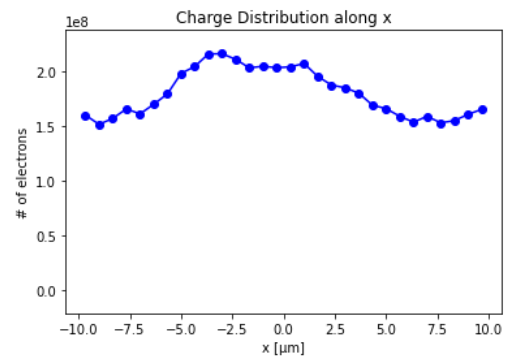
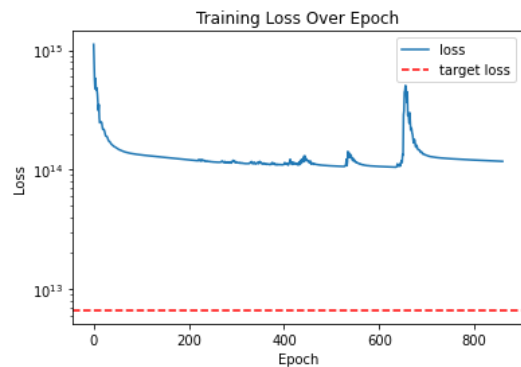


# GNN-based reconstruction

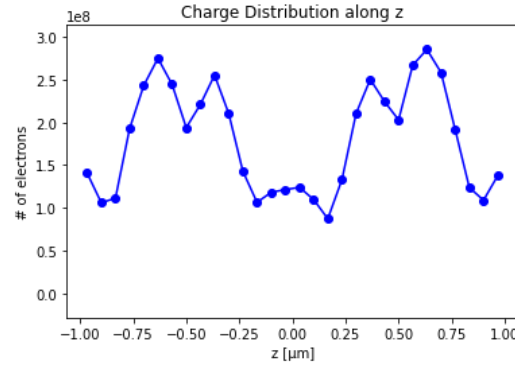
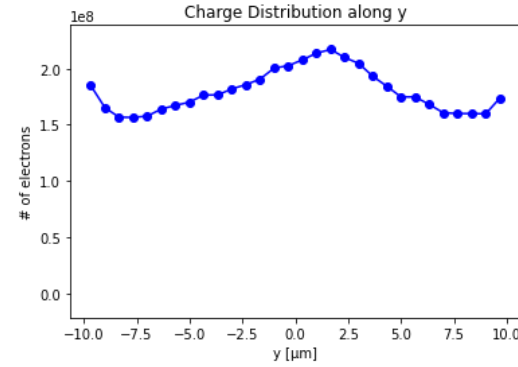
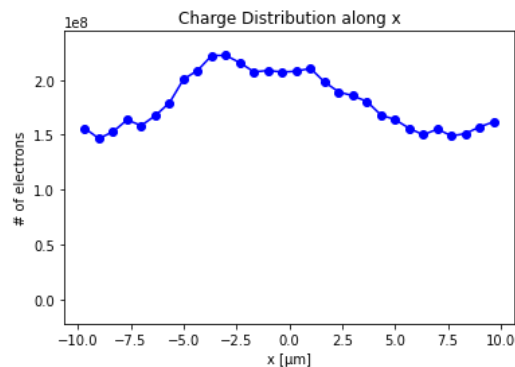
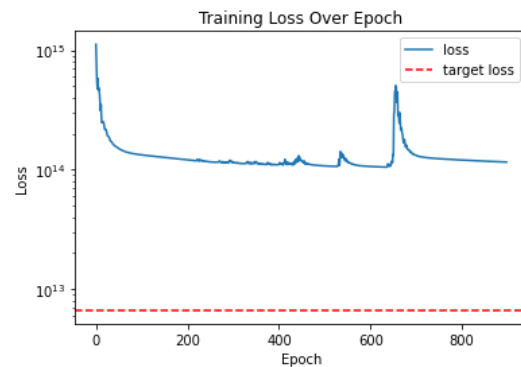


# Uniqueness discussion on GNN from seed (71)

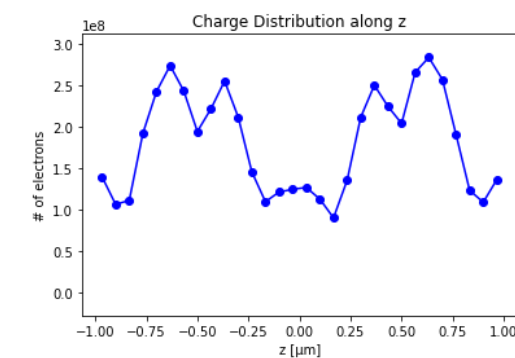
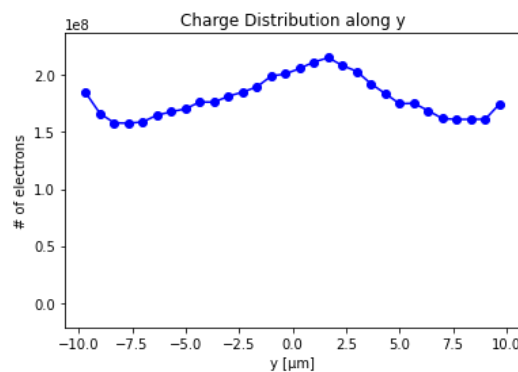
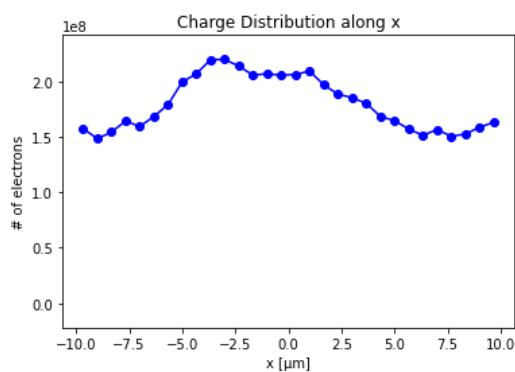
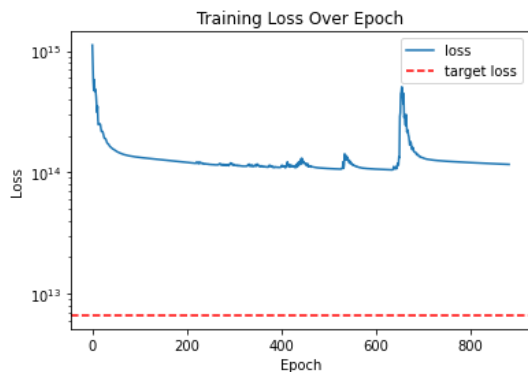
Solution 1



Solution 2

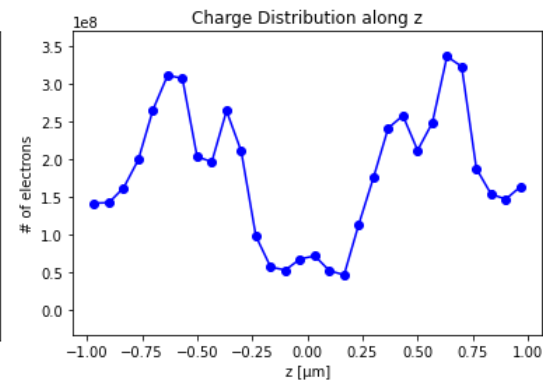
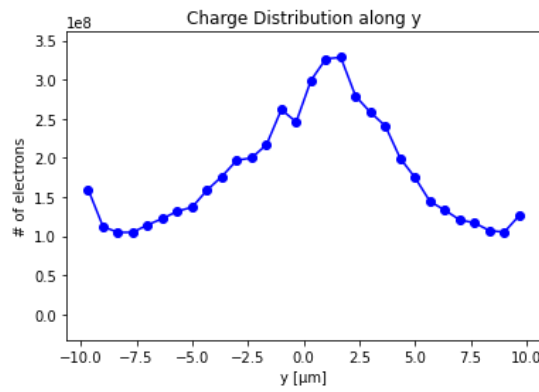
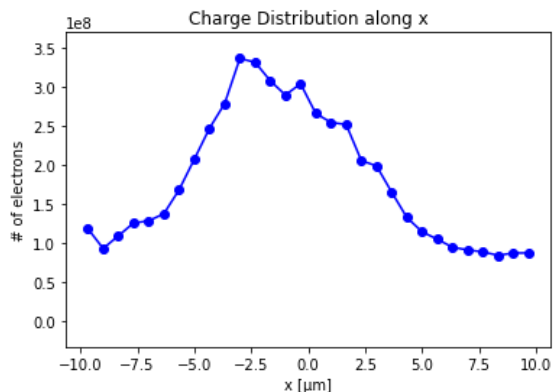
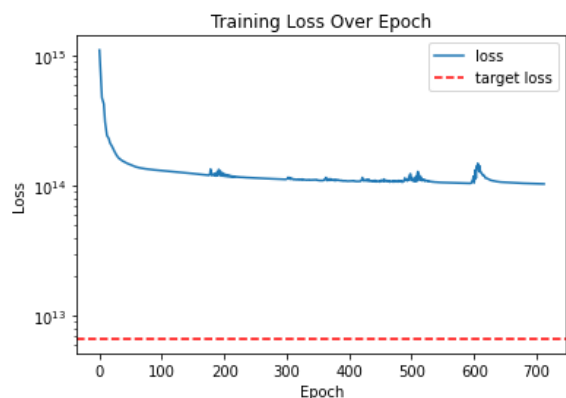


Solution 3

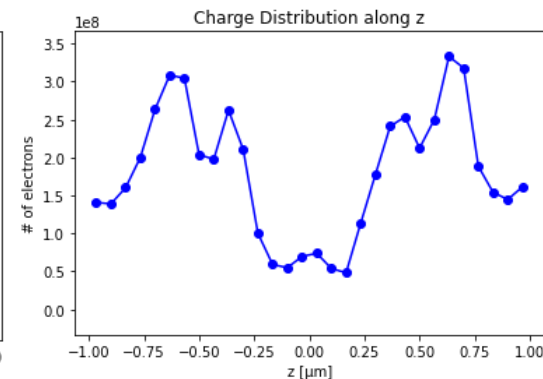
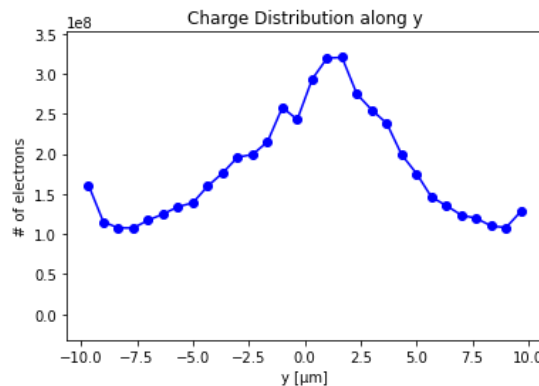
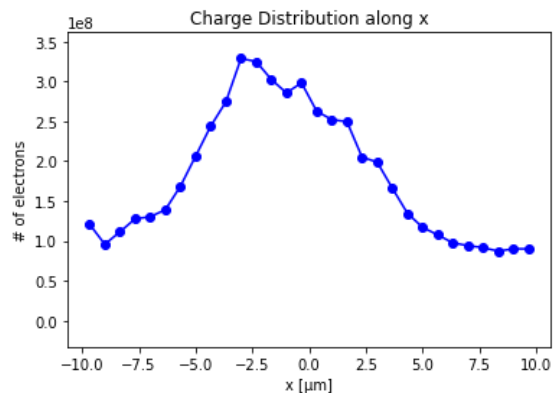
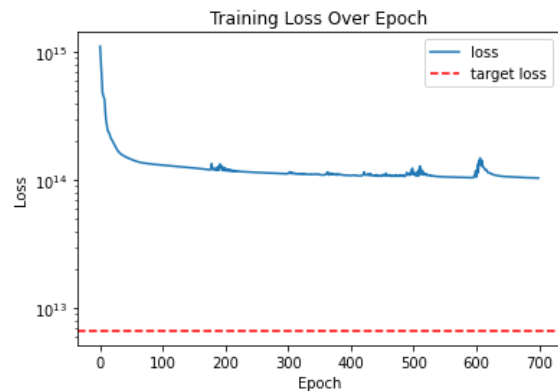


# Uniqueness discussion on GNN from seed (51)

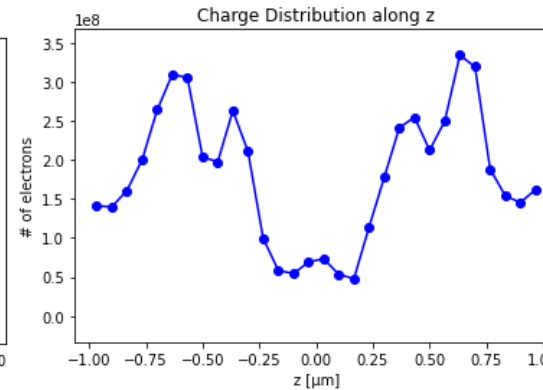
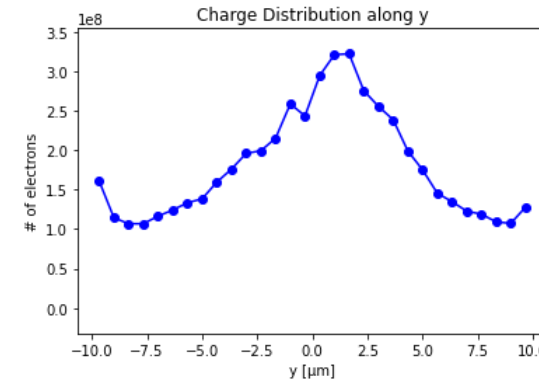
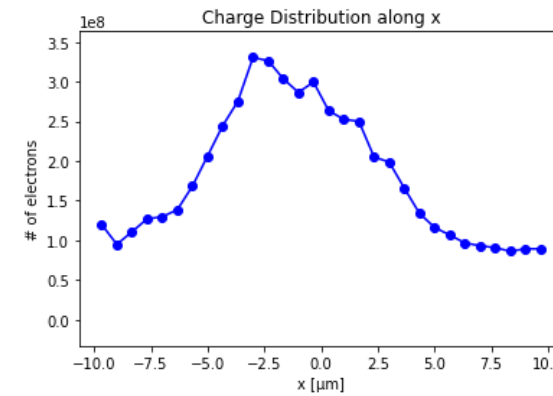
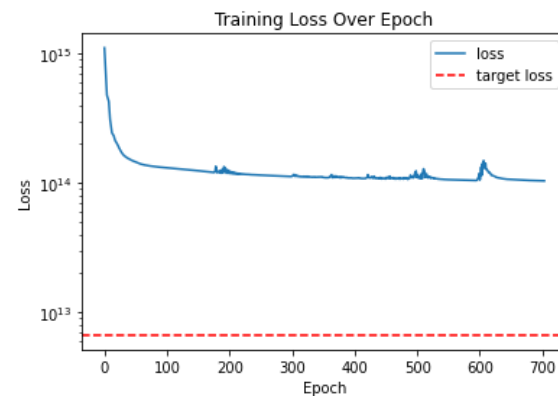
Solution 1



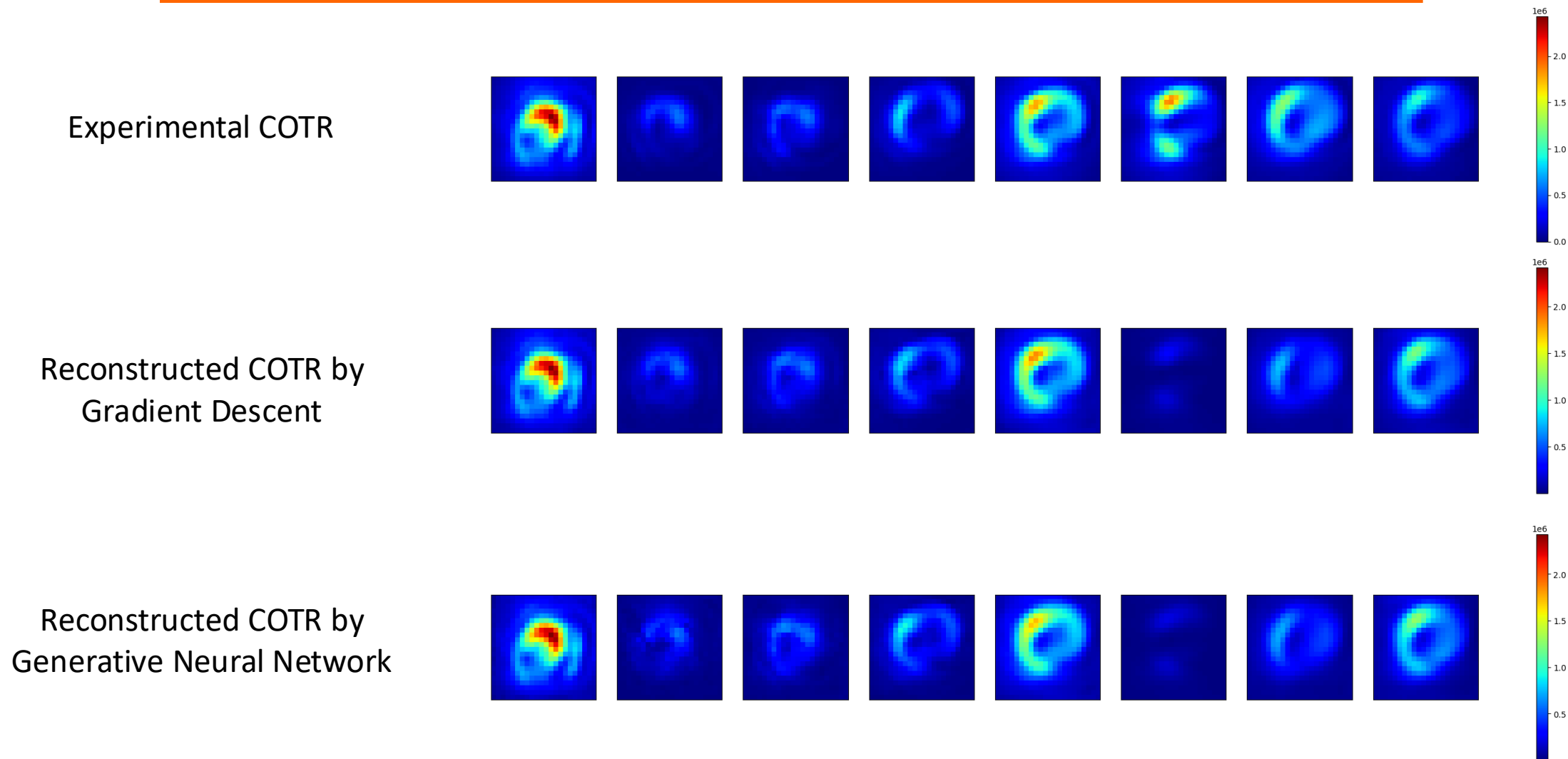
Solution 2



Solution 3

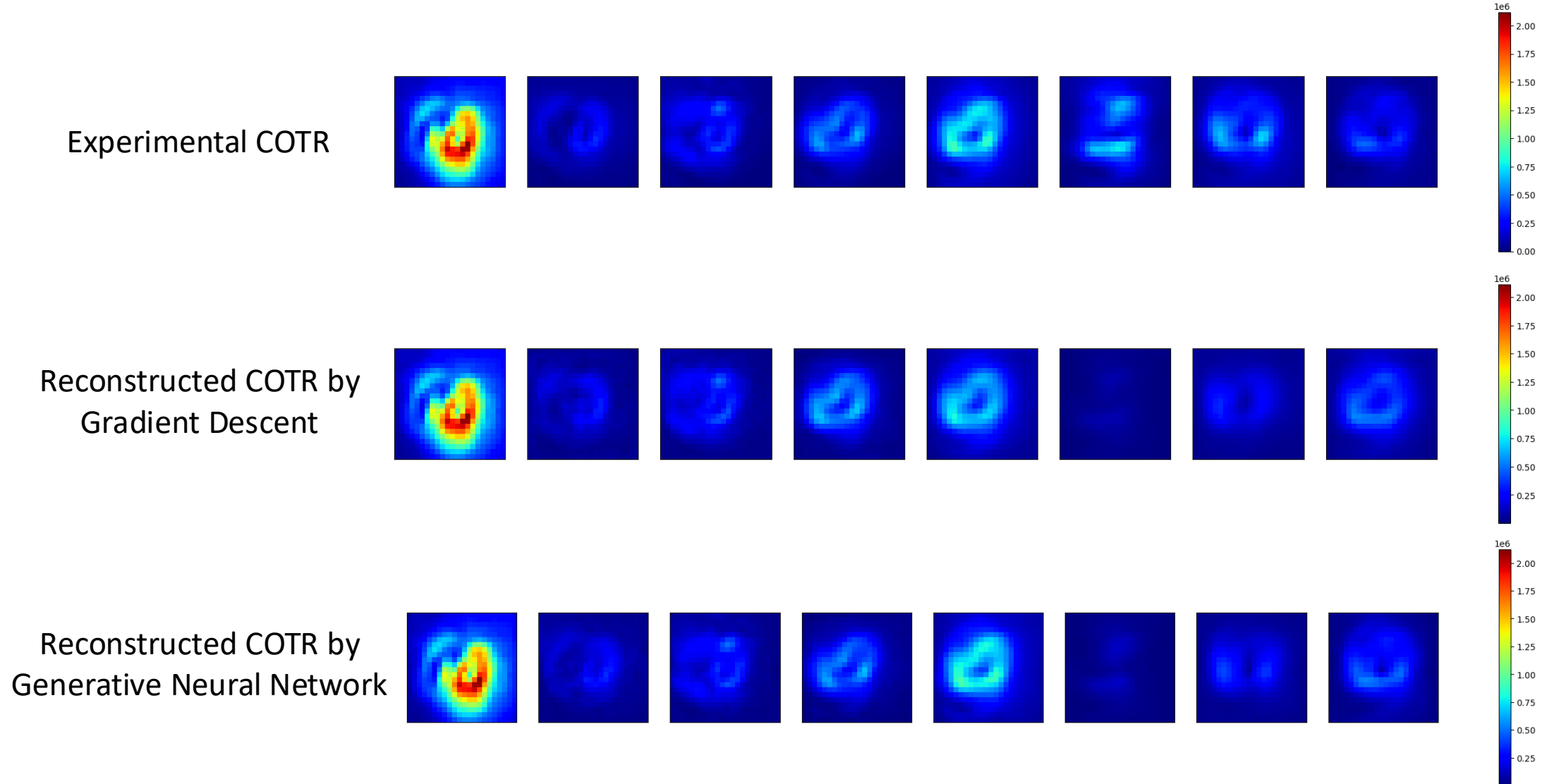


# Robustness of GD & GNN, shot 228



# Robustness of GD & GNN, shot 237

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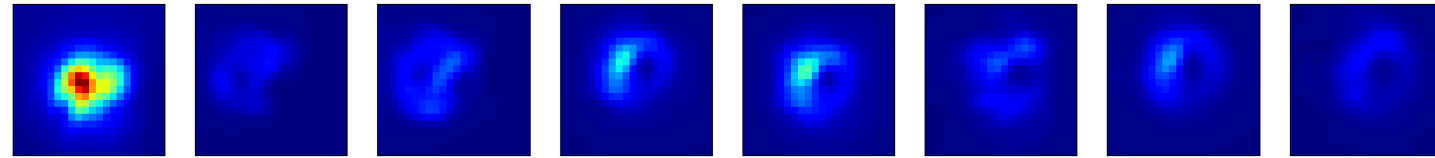




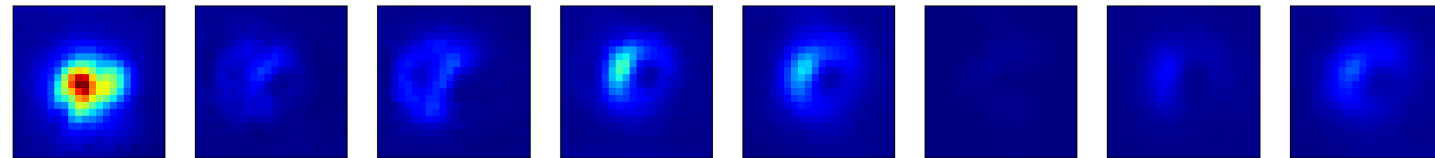
# Robustness of GD & GNN, shot 526

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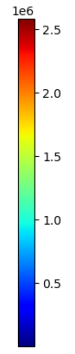
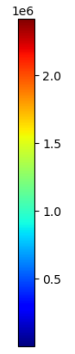
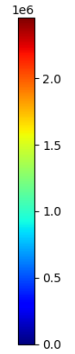
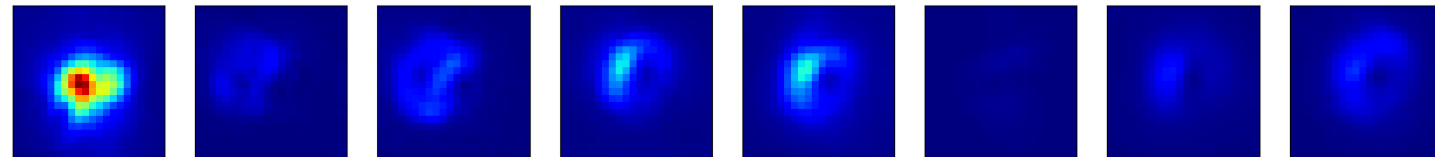
Experimental COTR



Reconstructed COTR by  
Gradient Descent



Reconstructed COTR by  
Generative Neural Network



# Conclusion & Discussion

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## Conclusion

1. In both methods, same seed leads to same reconstructed electron bunches; but different seeds lead to different reconstructed electron bunches.
2. Our methods show robustness on multiple shots.
3. Two-wavelength-figures don't match well in all situations.

## Discussion

1. Why loss stuck at a certain level? Model, initial condition, fine-tuned parameters
2. Other ways to describe electron bunches
3. Other use of NN: reduction of parameters, Physics-informed NN,
4. dataset generation
5. Initial parameters of electron bunches
6. Physically-reasonable converged electron bunches
7. Combination with prior knowledge of electron bunches, i.e. z- distribution